## edexcel

Mark Scheme (Results)
January 2016

Pearson Edexcel International GCSE Mathematics A (4MA0)
Paper 4H
Pearson Edexcel Certificate
Mathematics A (KMAO)
Paper 4H

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Types of mark
- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)
- Abbreviations
- cao - correct answer only
- ft - follow through
- isw - ignore subsequent working
- SC - special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- eeoo - each error or omission
- awrt -answer which rounds to
- No working

If no working is shown then correct answers normally score full marks
If no working is shown then incorrect (even though nearly correct) answers score no marks.

- With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.
If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.
Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.
If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.
If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.
If there is no answer on the answer line then check the working for an obvious answer.

- Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.
It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.
Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

- Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

Apart from Questions 9c, 11, 13, 22 and 23 (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

| Q | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 1 (a) | $2.14 \ldots \div 4.4$ | 0.4874(456952) | 2 | $\begin{array}{\|ll\|} \hline \text { M1 } & \text { for } 2.14 \ldots . \text { or } 4.4 \text { or } \frac{\sqrt{115}}{22} \\ \text { A1 } & \text { Accept if first four sig figs correct } \\ \hline \end{array}$ |
| (b) |  | 0.487 | 1 | B1 ft if (a) > 3 sig figs |
|  |  |  |  | Total 3 marks |

\(\left.$$
\begin{array}{|l|l|l|l|l|}\hline \mathbf{2} & \begin{array}{l}3 \times(-5)^{2}+4 \times-5 \\
\text { or } 3 \times(-5)^{2}-20 \text { or } 75\end{array} & 2 & \text { M1 } \begin{array}{l}\text { for correct substitution, brackets } \\
\text { essential }\end{array}
$$ <br>

\hline \& \& 55\end{array}\right]\) A1 | Total 2 marks |
| :--- |

\(\left.$$
\begin{array}{|c|l|l|l|l|}\hline \mathbf{3} & \begin{array}{l}8 \times 4(=32) \text { or } 1+9 \text { or } 10-1 \\
" 32 "-(3+1+5+5+2+3)(=13) \text { or } \\
(3+1+5+5+2+3)+" 10 "(=29)\end{array}
$$ \& 3 \& M1 <br>

\hline \& \& 3 and 10\end{array}\right]\)| A1A correct method to find the total <br> of the 2 missing numbers |
| :--- |
| If M0 scored then SCB1 for an <br> answer of two numbers with a <br> sum of 13 or two numbers that <br> give a range of 9 for the 8 cards |


| 4 | $\frac{2}{5} \times 30 \text { or } 0.4 \times 30$ | 12 | 2 | M1 <br> A1 (an answer of $\frac{12}{30}$ gains M1 only) |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Total 2 marks |
|  |  |  |  |  |  |
| 5 |  | $\begin{gathered} 110^{\circ} \\ \frac{\text { angles in a triangle total } 180^{\circ}}{\text { or corresponding angles }} \end{gathered}$ | 3 | M | Completely correct method seen (no isw) |
|  |  |  |  | A1 | SCB1 if M0 scored, B1 for AED stated or labelled as $110^{\circ}$ |
|  |  |  |  | B1 | At least one correct reason used |
|  |  |  |  |  | Total 3 marks |

$\left.\begin{array}{|l|l|l|l|l|}\hline \mathbf{6} & 0.5 \times(1+6) \text { or } 0.5 \times(4+9) & 2 & \begin{array}{l}\text { M1 } \\ \begin{array}{l}\text { for a correct method to find one } \\ \text { coordinate or for 1 coordinate } \\ \text { given correctly or for (6.5, 3.5) }\end{array} \\ \hline\end{array} & (3.5,6.5)\end{array}\right]$

| 7 (a) | $\begin{aligned} & \frac{12}{100} \times 30 \text { or } 0.12 \times 30 \text { or } 3.6 \\ & 30-" 3.6 " \end{aligned}$ | 26.4(0) | 3 | M1 <br> M1dep <br> A1 | M2 for $\frac{88}{100} \times 30$ or $0.88 \times 30$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $\frac{9}{0.12}$ or $\frac{9}{12} \times 100$ oe | 75 | 3 | M2 M1 for $\frac{9}{12}$ or $9=12 \%$ or $9=\frac{12}{100}$ oe <br> A1 (NB: if $75 \pm 9$ calculated, M2 only) |  |
|  |  |  |  |  | Total 6 marks |


| $\mathbf{8}$ (a) | $1-(0.2+0.05+0.15)$ or $1-0.4$ | 0.6 | 2 | M1 <br> A1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| (b) | $6+6 \times 4+6 \times 3+6 \times 12(=6+24+18+72)$ <br> or $6 \times 20$ or $\frac{6}{0.05}$ oe |  | 2 | M1ft$6+6 \times 4+6 \times 3+\frac{'^{\prime} 0.6^{\prime} \times 6}{0.05} \times 6$ <br> (allow M1 for 3 correct products <br> out of 4) |


| 9 (a) |  | $x^{2}+2 x$ | 1 | B1 | $2 x+x^{2}$ or $x 2+x^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | $4 x>3+7$ or $4 x>10$ | $x>2.5$ | 2 | M1 <br> A1 | for $4 x>3+7$ or $4 x>10$ or $4 x=3+7$ or $4 x=10$ or $x=2.5$ or $x<2.5$ or an answer of 2.5 following $x>2.5$ in working allow $x>\frac{10}{4}$ oe must have correct inequality sign |
| (c) | $3-5 m=8 \times 4$ or $3-5 m=32$ or $32+5 m=3$ |  | 3 | M1 | Multiplying both sides by 4 as a correct first step |
|  | $\begin{aligned} & -5 m=‘ 32 '-3 \text { or } 3-‘ 32 ’=5 m \\ & -5 m=29 \text { or }-29=5 m \end{aligned}$ | -5.8 |  | M1 | for isolating $5 m$ or $-5 m$ in a correct equation <br> oe eg $\frac{-29}{5}$ dependent on at least M1 |
|  | Alternative for (c) |  |  |  |  |
| (c) | $\frac{-5 m}{4}=8-\frac{3}{4}$ or $\frac{5 m}{4}=\frac{3}{4}-8$ | -5.8 | 3 | M1 | For using quarters (or a multiple of 4) and isolating the term in $m$ in a correct equation |
|  | $-5 m=\left(8-\frac{3}{4}\right) \times 4 \text { or } 5 m=\left(\frac{3}{4}-8\right) \times 4$ |  |  | M1 | For isolating $5 m$ or $-5 m$ in a correct equation. |
|  |  |  |  |  | oe eg $\frac{-29}{5}$ dependent on at least M1 |
|  |  |  |  |  | Total 6 marks |


| 10 | $\frac{24.5}{7} \times 2(=7)$ or $\frac{24.5}{7} \times 6(=21)$ or $\frac{24.5}{7} \times 8(=28)$ |  | 3 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | $\frac{24.5}{7} \times 2+\frac{24.5}{7} \times 6+24.5(7+21+24.5)$ |  |  | M1fully correct method <br> $\left[M 2\right.$ for $\left.\frac{24.5}{7} \times(7+6+2)\right]$ |
|  |  |  |  | A1 |


| $\mathbf{1 1}$ | Eg. $4 x=14$ or $4 y=-2$ or $-4 y=2$ <br> or $5(3-y)+y=17$ or $5 x+3-x=17$ or <br> $x+17-5 x=3$ | $x=3.5, y=-0.5$ | M1 for correctly eliminating 1 variable |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | Aloe Aloe dep on M1 |

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{3}{*}{12} \& $m=-2$

$c=13$ \& \multirow{3}{*}{$y=-2 x+13$} \& \multirow[t]{3}{*}{3} \& M1 \& For recognising gradient $=-2$, eg $y=-2 x+c$ where $c \neq 4$ \& M2 for

$$
7=-2 \times 3+c
$$ <br>

\hline \& \multirow{2}{*}{$c=13$} \& \& \& \multicolumn{3}{|l|}{A1 oe e.g. $y-7=-2(x-3)$} <br>
\hline \& \& \& \& \multicolumn{3}{|c|}{SCB2 for $-2 x+13$} <br>
\hline \& \& \& \& \& \& Total 3 marks <br>
\hline
\end{tabular}

| 13 | $180-\frac{360}{10} \text { or } \frac{(10-2) \times 180}{10} \text { or } 144 \mathrm{oe}$ | 108 | 4 | M1 | Unless inconsistently labelled |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\frac{180-' 144 '}{2} \text { or } 18$ |  |  | M1 | Or M2 for $144-(180-144)$ |
|  | ' $144{ }^{\prime}-2 \times 18$ ' |  |  | M1 |  |
|  |  |  |  | A1 | dep on M1 |
|  | Alternative |  |  |  |  |
|  | Pentagon approach - drawing in a pentagon or a statement recognising that the required angle is one of a regular pentagon |  | 4 | M1 | May be implied by further work |
|  | $180-\frac{360}{5} \text { or } \frac{(5-2) \times 180}{5}$ |  |  | M2 | (M1 for exterior angle of pentagon as long as not seen as interior angle or given as answer) |
|  |  | 108 |  | A1 | dep on M1 |
|  |  |  |  |  | Total 4 marks |


| $\mathbf{1 4}$ (a) | $5 \times \frac{10}{4}$ oe |  | 2 | M1 |
| :---: | :--- | :---: | :---: | :--- |
| (b) | $18 \div \frac{10}{4}$ oe |  |  | A1 |
| (c) |  | 7.2 | 2 | M1 |


| 15 (a) |  | Points correct <br> Curve or line <br> segments joining <br> points | 2 | B1$\pm \frac{1}{2}$ square <br> ft curve/line segments from points <br> if 3 or 4 plotted correctly or if all <br> 5 points are plotted consistently <br> within successive 10 unit intervals <br> at the correct heights. |
| :---: | :--- | :--- | :--- | :--- | :--- |
| (b) | 30 (or 30.5) indicated on cf graph or stated, or <br> vertical line corresponding to height $=30$ (or 30.5$)$ <br> $\left( \pm \frac{1}{2}\right.$ sq) | $157-159$ | 2 | M130 or (30.5) indicated on cf graph <br> or stated. |
| (c) | Vertical line or mark drawn at 174 cm or <br> horizontal line corresponding to height $=174 \mathrm{~cm}$ <br> $\left( \pm \frac{1}{2}\right.$ sq) | 5 or 6 | A1ftIf M1 scored ft from a cf graph <br> If M1 not scored, ft only from <br> correct curve. |  |
|  |  | 174 indicated on the cf graph |  |  |


| 16 (a) |  | $6 x-12$ | 2 |  | for $6 x$ or -12 (allow $2 \times 3 x$ for $6 x$ ) fully correct |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) | ' $6 x-12$ ' $=18$ oe | $(5,23)$ | 3 | M1ft <br> M1 <br> A1 | ft equation in form $a x+b$ $(a \neq 0, b \neq 0)$ <br> Full method to solve their equation $(5,23)$ |
|  |  |  |  |  | Total 5 marks |


| 17 (a) |  | $\frac{2 e^{2}}{f^{4}}$ | 2 | B2 | Fully correct. Accept $2 e^{2} f^{-4}$ B1 for 2 out of 3 correct terms in a product or quotient |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  |  | 2 | M1 | $\begin{aligned} & \text { for } 2\left(y^{2}-36\right) \text { or }(2 y-12)(y+6) \\ & \text { or }(2 y+12)(y-6) \end{aligned}$ |
|  |  | $2(y+6)(y-6)$ |  | A1 |  |
| (c) | $\frac{(p-3)(2 p+5)}{p(p-3)}$ | $2 p+5$ | 3 |  | $(p-3)(2 p+5)$ |
|  |  |  |  | M1 | $p(p-3)$ or $(p+0)(p-3)$ |
|  |  | $p$ |  | A1 | oe e.g. $2+\frac{5}{p}$ (NB: if candidates incorrectly cancel a correct algebraic fraction they lose the A mark) |
|  |  |  |  |  | Total 7 marks |



\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[t]{9}{*}{19} \& $$
\tan 38=\frac{Q S}{8.4} \text { or } \tan 52=\frac{8.4}{Q S} \text { or } \frac{Q S}{\sin 38}=\frac{8.4}{\sin 52}
$$ \& \multirow[b]{4}{*}{9.12} \& \multirow[t]{4}{*}{4} \& M1 \& Must be a correct equation <br>
\hline \& $$
\begin{aligned}
& (Q S=) 8.4 \tan 38 \text { or }(Q S=) 8.4 / \tan 52 \text { or } \\
& (Q S=) \frac{8.4 \sin 38}{\sin 52} \quad(=6.56 \ldots)
\end{aligned}
$$ \& \& \& M1 \& A correct calculation for $Q S$ or 6.56... <br>
\hline \& $$
(Q R=) \frac{\prime 6.56 '}{\cos 44} \text { or }(Q R=) \frac{6^{\prime} 6.56 '}{\sin 46}
$$ \& \& \& M1 \& A correct calculation with their $Q S$ for length $Q R$ <br>
\hline \& $Q R=9.12$ (336459) \& \& \& A1 \& Awrt 9.12 <br>
\hline \& Alternative \& \multirow[t]{5}{*}{9.12

9.12} \& \multirow{5}{*}{4} \& \& <br>

\hline \& $$
\cos 38=\frac{8.4}{P Q} \text { or } \sin 52=\frac{8.4}{P Q}
$$ \& \& \& M1 \& Must be a correct equation <br>

\hline \& $$
(P Q=) \frac{8.4}{\cos 38} \text { or }(P Q=) \frac{8.4}{\sin 52}(=10.65 \ldots)
$$ \& \& \& M1 \& A correct calculation for $P Q$ Or 10.6\7... <br>

\hline \& $$
(Q R=) \frac{' 10.65 . .{ }^{\prime}}{\sin 46} \times \sin 38
$$ \& \& \& M1 \& A correct calculation with their $P Q$ for length $Q R$ <br>

\hline \& $Q R=9.12$ (336459) \& \& \& A1 \& Awrt 9.12 <br>
\hline \& \& \& \& \& Total 4 marks <br>
\hline
\end{tabular}

| 20 | $\begin{aligned} & B P \times 10=15 \times 8 \text { or }(10+A B) \times 10=15 \times 8 \text { oe } \\ & (B P=)(15 \times 8) \div 10(=12) \text { oe or } \\ & 10 A B=120-100 \text { oe or } \\ & 10+A B=(15 \times 8) \div 10 \text { oe } \end{aligned}$ | 2 | 3 | M1 <br> M1 <br> A1 | for a correct equation <br> a correct calculation for $B P$ or a correct simplified equation for $A B$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Total 3 marks |


| 21 | $\begin{aligned} & \left(B C^{2}=\right) 4.8^{2}+6.4^{2}-2 \times 4.8 \times 6.4 \times \cos 123^{\circ} \\ & \left(B C^{2}=\right) 23.04+40.96+33.46 . . \mathrm{oe} \\ & (=97.4(6262231)) \end{aligned}$ | 9.87 | 3 | M1 <br> M1 <br> A1 | Correct use of cosine rule to find $B C^{2}$ <br> Correct order of operations \& correct values <br> awrt 9.87 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Total 3 marks |


| 22 | $\begin{aligned} & \frac{6(x+1)-6(x-2)}{(x-2)(x+1)} \text { or } \\ & \frac{6(x+1)}{(x-2)(x+1)}-\frac{6(x-2)}{(x-2)(x+1)}(=1) \text { oe } \\ & 6(x+1)-6(x-2)=(x+1)(x-2) \text { oe } \\ & \left(18=x^{2}-x-2\right) \\ & x^{2}-x-20(=0) \\ & (x+4)(x-5)(=0) \end{aligned}$ | $x=5, x=-4$ | 5 | M1 <br>  <br> M1 <br>  <br>  <br> A1 <br>  <br> M1 <br>  <br> A1 | Correct single fraction or 2 fractions with the same correct common denominator If expanded, condone 1 error in numerator <br> Correct removal of denominator (M2 if a candidate goes straight to this stage) if expanded, condone 1 error <br> Correct 3 part quadratic (eg $x^{2}-x-20(=0)$ or $x^{2}-x=20$ or $x^{2}=x+20$ ) <br> $(x+4)(x-5)(=0)$ or <br> a fully correct substitution into the quadratic formula $\mathrm{eg} \frac{--1 \pm \sqrt{(-1)^{2}-4 \times 1 \times-20}}{2 \times 1}$ <br> Condone no brackets around -1 or $\frac{1 \pm \sqrt{81}}{2}$ dep on last M1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Total 5 marks |


| 23 | Allow use of $\pi=3.14$.. consistently throughout, for either scheme, but not a rounded decimal for the radius $\pi \times(4 \sqrt{3})^{2}$ or $2 \pi \times(4 \sqrt{3})^{2}$ or $2 \pi \times 4 \sqrt{3} h$ | $7 \sqrt{2}-4 \sqrt{3}$ | 5 | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \end{aligned}$ | correct expression for curved surface area or area of 1 or 2 circles (condone missing brackets around $4 \sqrt{3}$ forM1M1) |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $2 \pi \times(4 \sqrt{3})^{2}+2 \pi \times 4 \sqrt{3} h(=56 \pi \sqrt{6})$ |  |  |  | correct expression for total surface area (candidate may have already divided by $\pi$ or do so at any stage if already working in an equation) |
|  | $\begin{aligned} & 96 \pi+8 \pi \times \sqrt{3} h(=56 \pi \sqrt{6}) \\ & (h=) \frac{56 \pi \sqrt{6}-2 \pi(4 \sqrt{3})^{2}}{2 \pi(4 \sqrt{3})} \end{aligned}$ |  |  | M1 | A correct simplified expression for total the total surface area or a correct expression for $h$ |
|  | $(h=) \frac{56 \pi \sqrt{6}-96 \pi}{8 \pi \sqrt{3}} \text { or }(h=) \frac{56 \sqrt{6}-96}{8 \sqrt{3}} \text { oe }$ |  |  | M1 | correct rearrangement in terms of $h$ and simplified as a quotient |
|  |  |  |  | A1 | dep on M2 |
|  | Alternative |  |  |  |  |
|  | $2 \pi r h+2 \pi r^{2}$ or $2 \pi r h+\pi r^{2}$ | $7 \sqrt{2}-4 \sqrt{3}$ | 5 | M1 | A correct algebraic expression for the csa +2 circles or csa +1 circle |
|  | $\begin{aligned} & 2 r h+2 r^{2}=56 \sqrt{6} \text { or } r h+r^{2}=28 \sqrt{6} \text { or } \\ & 2 \pi r(h+r)=56 \pi \sqrt{6} \text { or } 2 \pi r h=56 \pi \sqrt{6}-2 \pi r^{2} \end{aligned}$ |  |  | M1 | A correct equation and correct division by $\pi$ or $2 \pi$ or a correct factorisation or correctly isolating term in $h$ |
|  | $(h=) \frac{56 \pi \sqrt{6}}{2 \pi r}-r \text { or }(h=) \frac{56 \pi \sqrt{6}-2 \pi r^{2}}{2 \pi r} \text { oe }$ |  |  | M1 | A fully correct expression for $h$ |
|  | $(h=) \frac{56 \pi \sqrt{6}}{2 \pi 4 \sqrt{3}}-4 \sqrt{3} \text { or }(h=) \frac{56 \pi \sqrt{6}-96 \pi}{8 \pi \sqrt{3}} \text { oe }$ |  |  | M1 | Correct substitution of $r$ into a correct equation or expression for $h$ |
|  |  |  |  | A1 | dep on M2 |
|  |  |  |  |  | Total 5 marks |



| $\mathbf{2 5}$ | 32 or 3.2 or $10^{10 k}$ <br> $32 \times 10^{10 k}$ <br> $3.2 \times 10^{10 k+1}$ | 3 | M1 |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  | $3.2 \times 10^{10 k+1}$ |  | M1 |

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